3. Suppose 2 firms compete on quantity with inverse demand function $p=1-b Q$ where $Q$ is total output. They have zero costs. Demand varies over time. Specifically, the parameter $b$ is either $b_{H}$ or $b_{L}$ with equal probability each time period, with $b_{H}>b_{L}>0$. Both firms know the level of demand at the start of the period. Show that in the indefinitely repeated game, with rate of time preference $\delta$, the monopoly level of output can be supported as a subgame perfect equilibrium. What strategies support this outcome? What would be the optimal deviation? Hence, calculate the lowest value of the rate of time preference $\delta$ for which the joint profit maximizing output is possible.
