

# **Voting versus Lobbying**

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## *The Setting*

- political contest between two groups providing or promising effort
- lobbying groups, political parties
- consider different mechanisms for resolving the contest
  - winner pays – first or second price auction: example – a politician to be bribed – common in the lobbying literature
  - everyone pays: example – an election, warfare – common in the voting literature
    - all-pay auction where greater effort wins
    - linear Tullock contest success function where greater effort increases the chance of winning: true in warfare, in voting we have weather, intervention of courts, way votes are counted, proportional representation and so forth

## ***Empirical Applications of this Class of Models***

- Coate-Conlin: referendum voting in Texas
- Esteban-Ray-Mayoral: ethnic conflict

## ***Are Large or Small Groups More Effective?***

- Olson, Becker, Levine/Modica others argue that smaller groups are more effective at lobbying
- Levine/Mattozzi, others argue that larger groups are more effective at voting
- When groups of different sizes compete for the same prize when is the larger or smaller group more likely to be successful?
- Why should it be different for voting and lobbying?
- What factors determine the effectiveness of groups of different sizes?

## *Duties versus Chores*

- effort provision a *duty*: we view voting as a civic duty so we receive a benefit for doing our duty that exceeds at least some of the cost of participating

duty in the broad sense: a political demonstration or protest might be an enjoyable event - to be outdoors in good weather, meet new people, chant, march and sing

- effort provision a *chore*: a fixed cost of participation

cannot simply write a check for 32 cents to “anti-farm subsidies” must find the appropriate organization, learn about them, join up - and they have to vet me, process my application and so forth

considerable cost incurred even as I contributed absolutely nothing to the lobbying effort

- tend to think of voting as a duty and lobbying as a chore, but the cost structure is the fundamental distinction

## ***The Main Results***

- difference between voting and lobbying
  - duty (voting) versus chore (lobbying)
  - all-pay (voting) versus winner-pays (lobbying)
- duty favors large groups while chores favor small groups
- all-pay versus winner-pays does not matter
- since it is the cost function that matters we examine the micro-foundations of the cost function
- there are several models of group behavior – do they give rise to different cost functions with different conclusions concerning duty and chores?
- (no)

## ***The Political Contest Between Groups***

two groups  $k = S, L$  of size  $N_L > N_S$  compete for a common prize worth  $V$  to the group and  $v_k = V/N_k$  to each group member.

only difference between groups is their size

groups behave as single individuals

choose a social norm in the form of a per capita effort level  $0 \leq \varphi_k \leq 1$

- marginal cost of per capita effort up to a threshold  $\underline{\varphi} \geq 0$  is  $-f < 0$
- further effort requires a per capita fixed cost  $F \geq 0$  plus a marginal cost of  $c > 0$

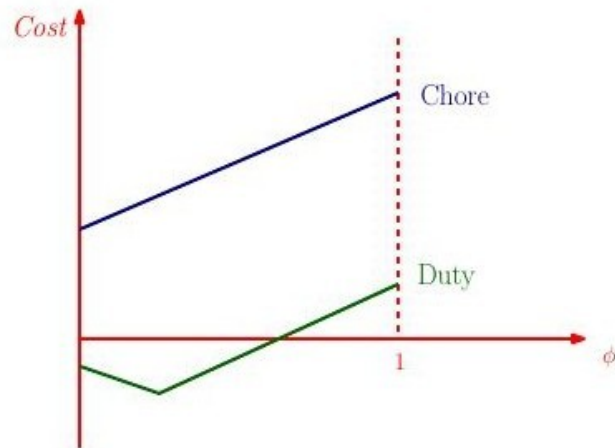
group may “burn money” by choosing to pay the fixed cost without providing additional effort

## Duties versus Chores

only allow two cases:

- effort a *duty*:  $\underline{\varphi} > 0$  and  $F = 0$
- effort is a *chore*:  $\underline{\varphi} = 0$  and  $F > 0$

we will examine the micro-foundations of the cost function later





## ***Bids, Strategies and Payoffs***

social norm  $\varphi_k$  in per capita terms results in total effort or *bid*  $b_k = N_k \varphi_k$

pure strategy for group  $k$  is choice of accepting the fixed cost  $q_k \in \{0, 1\}$  and a social norm  $\varphi_k$  satisfying the feasibility condition that  $q_k = 1$  if  $\varphi_k > \underline{\varphi}$

if group has probability  $p_k$  of winning the prize and follows pure strategy  $q_k, \varphi_k$  it receives per capita utility

$$p_k v_k - q_k F - c \max\{0, \varphi_k - \underline{\varphi}\} + f \min\{\varphi_k, \underline{\varphi}\}$$

## Willingness to Pay

*willingness-to-pay* is the greatest amount of effort group would be willing to provide to get the prize for certain.

$$W_k = \begin{cases} N_k \varphi & \text{if } V < N_k F \\ N_k \varphi + \frac{\bar{V} - N_k F}{c} & \text{if } V \in [N_k F, N_k((1 - \varphi)c + F)] \\ N_k & \text{if } V > N_k((1 - \varphi)c + F) \end{cases}$$

benefit of duty  $f$  does not figure in because group can receive that benefit regardless of whether or not it wins the prize

if  $V \leq N_k F$  for both groups we say that both groups are *disadvantaged*

otherwise a group with the highest willingness to pay is called *advantaged* and the other group *disadvantaged*

## ***Size of the Prize***

- prize is small if  $V < FN_S$
- prize is medium if  $N_SF < V < FN_L + cN_S$
- prize is large if  $V > FN_L + cN_S$

## **Group Advantage**

**Theorem:** *For a chore with a small prize both groups are disadvantaged. For a chore with a medium prize the small group is advantaged. For a large prize or a duty the large group is advantaged.*

## ***Allocation Mechanisms***

*allocation mechanism* determines the award of the prize and the contributions of the two groups based on their bids

1. Second-price auction. The highest bidder wins and provides an effort contribution equal to the bid of the lower bidder.
2. First-price auction. The highest bidder wins and provides an effort contribution equal to their own bid.
3. All-pay auction. The highest bidder wins and both bidders provide an effort contribution equal to their own bid.
4. Linear Tullock contest. Group  $k$  wins the prize with probability

$$p_k = \frac{b_k}{b_k + b_{-k}}$$

both bidders provide an effort contribution equal to their own bid.

- for chores if neither group chooses to incur fixed cost the prize is canceled and both groups receive zero
- for auctions if there is a tie the winner is determined endogenously.

## *Equilibrium*

Nash equilibrium of the game between groups (two-player game) with the following refinements:

1. Second-price auction: weakly undominated strategies
2. First-price auction: the “honest bidding” refinement from menu auctions – a bid that loses with probability one must be equal to the willingness-to-pay.
3. All-pay auction: none
4. Linear Tullock contest: pure strategy equilibrium.

## Tripartite Auction Theorem

$d$  the disadvantaged group

if  $W_d \geq N_{-d}\underline{\varphi}$  it costs the advantaged group  $c(W_d - N_{-d}\underline{\varphi}) + N_{-d}F$  to match the bid of the disadvantaged group

if  $W_d < N_{-d}\underline{\varphi}$  it costs nothing to overmatch the bid of the disadvantaged group

*surplus* is the difference between the value of the prize and cost of matching the bid of the disadvantaged group if this is positive, zero otherwise.

**Theorem:** *In the second-price, first-price and all-pay auction a disadvantaged group gets 0 and an advantaged group gets the surplus. The expected effort provided is the same for the second-price and first-price auction and no greater for the all-pay auction. If  $W_d > N_{-d}\underline{\varphi}$  then the expected effort provided is strictly less for the all-pay auction*

## ***Observations***

small group gets a positive surplus when there is a medium prize and a chore: fungibility (Levine/Modica) and resource constraints

rent dissipation: if the value of the prize is medium and groups are of similar size then value of prize dissipated

when effort has value to a recipient (for example to a politician who receives it as a bribe) then auction is preferred



## ***Linear Tullock Contest***

The disadvantaged group does not get zero but still gets less than the advantaged group

## ***Costly Participation and Free-riding***

- contests are not between individuals but between large groups
- farm lobby in the United States: two million farms
- enormous public goods problem: in voting theory called the paradox of voting
- chances of an individual vote changing the outcome of an election are so small that the incentive to vote is negligible – so indeed, why does anybody bother?
- why do farmers contribute to lobbying efforts when their individual effort makes little difference?
- everybody of course would like their group to win the contest – but of course would much prefer that everyone else contribute to the effort while they do not

## A Public Good Game

a simple within group game for the Tullock case

with Tullock contest fixed cost is paid if and only if  $\varphi^k > \underline{\varphi}$  and social norm is just  $\varphi^k$  with  $q(\varphi^k)$  being 0 if  $\varphi^k \leq \underline{\varphi}$  and being 1 if  $\varphi^k > \underline{\varphi}$

fix pure strategy of the other group  $-k$  and let  $p_k(N_k\varphi_k)$  be the probability that group  $k$  wins.

$k$  has members  $i = 1, 2, \dots, N_k$  each chooses effort level  $\phi^i \in [0, 1]$

effect of individual effort on the outcome is sufficiently small that individuals care only about their costs (no pivotality)

utility of an individual  $i$  who chooses  $\phi^i$  is negative of cost

$$C(\phi^i) = q(\phi^i)F + c \max\{0, \phi^i - \underline{\varphi}\} - f \min\{\phi^i, \underline{\varphi}\}$$

so everyone contributes the minimum

huge empirical literature saying “this is not true”

## Group Utility

group utility  $V_k(\phi^i, \varphi_k)$  when member  $i$  provides effort  $\phi^i$  and the other members use the social norm  $\varphi_k$

$$V_k(\phi^i, \varphi_k) = p_k(\phi^i + (N_k - 1)\varphi_k)V - (N_k - 1)C(\varphi_k) - C(\phi^i).$$

we can reiterate that given  $\varphi_k$  the optimal choice of  $\phi^i$  is  $\underline{\varphi}$

## ***Behavioral Theory 1 of 3: Rule Consequentialism***

each group member asks what would be in the best interest of the group

what pair  $\varphi^i, \varphi_k$  would maximize  $V_k(\varphi^i, \varphi_k)$ ?

assume a unique symmetric solution with  $\varphi^i = \varphi_k$

each member “does their part” by implementing  $\varphi^i = \varphi_k$

- conceptually supposed to capture the idea that it is unethical to free ride
- widely used in voting and implicitly used in lobbying literature

## ***Behavioral Theory 2 of 3: Partial Altruism***

individual objective function a weighted average of the group utility and own utility with weight  $0 \leq \lambda \leq 1$  a measure of selfishness

$$U_k(\phi^i, \varphi_k) = (1 - \lambda)V_k(\phi^i, \varphi_k) - \lambda C(\phi^i).$$

look for Nash equilibrium

$\lambda = 0$  complete altruism, not the same as rule-consequentialism due to possibility of coordination failure

$\lambda = 1$  complete selfishness

members are willing to bear some cost of contributing if they are altruistic enough

some quantitative problems with this approach including that it requires a level of altruism incompatible with evidence from other spheres of behavior

## ***Behavioral Theory 3 of 3: Peer Pressure***

- usually public good problems are overcome by coercion – mandatory voting laws, a military draft
- formal legal channels not so relevant for lobbying, nor indeed for voting
- coercion in the form of peer pressure is common

## ***Peer Pressure with an Endogenous Social Norm***

group colludes to maximize  $V_k(\varphi^i, \varphi_k)$  but group members must be coerced through punishment if they do not contribute their share

for a given individual social norm  $\varphi^i \in [0, 1]$  the group has a monitoring technology which generates a noisy signal of whether or not a member complies with the norm, that is, chooses  $\phi^i = \varphi^i$

signal is  $z^i \in \{0, 1\}$

0 means “good, followed the social norm”

1 means “bad, did not follow the social norm”

if member  $i$  does violate the social norm so  $\phi^i \neq \varphi^i$  then the signal is 1 (bad) for sure

if the member does follow the social norm  $\phi^i = \varphi^i$  the signal is 1 (good) with probability  $\pi$



## Crime and Punishment

bad signal received group member receives a punishment of size  $P^i$

optimal deviation is  $\phi^i = \underline{\varphi}$

social norm incentive compatible

$$-\pi P^i \geq C(\varphi^i) + \underline{\varphi}f - P^i$$

a colluding group acts to minimize the punishment cost so chooses

$$P^i = [C(\varphi^i) + \underline{\varphi}f]/(1 - \pi)$$

cost (of punishing the innocent) is

$$[C(\varphi^i) + \underline{\varphi}f]\pi/(1 - \pi)$$

## Accounting for Enforcement Costs

utility of the group taking account of enforcement costs

$$V_k(\varphi^i, \varphi_k) - ((N_k - 1)C(\varphi_k) + C(\varphi^i) + N_k \underline{\varphi} f) \pi / (1 - \pi)$$

equivalent to

$$W(\varphi^i, \varphi_k) = (1 - \pi)V_k(\varphi^i, \varphi_k) - \pi ((N_k - 1)C(\varphi_k) + C(\varphi^i))$$

group colludes to maximize with respect to both arguments

$W(\varphi^i, \varphi_k)$  is maximized with respect to  $\varphi^i$  only if

$$(1 - \pi)V_k(\varphi^i, \varphi_k) - \pi C(\varphi^i)$$

is maximized with respect to  $\varphi^i$

which is a solution to the partial altruism model with  $\lambda = \pi$

so often the details of the behavioral model is not that significant

## ***Indivisibility and Monitoring***

- examine the case where the effort is indivisible
- in voting a natural assumption: either a member votes or does not vote but does not cast half a vote
- lobbying often the group asks for a fixed levy of time, effort, or money, and treating the level of contribution of exogenous the issue for members is then whether or not to participate
- allow for *ex post* differences at the time the participation decision is made
- on election day a group member is in the hospital, a member of a lobbying group is suffering financial distress
- look at extensive margin (how many participate) rather than intensive margin (how much each contributes)

## ***Types and Costs***

group members draw types  $y^i$  uniformly distributed on  $[0, 1]$

may contribute 0 effort at 0 cost or they may contribute a single unit of effort at a cost of  $d(y^i)$  where we assume the types are ordered so that this is a non-decreasing function

specifically a linear function

$$d(y^i) = d_0 + \gamma y^i$$

$d_0$  negative a duty, positive a chore

where  $\gamma > \max\{0, -d_0\}$

common in the voting literature (in the duty case)

## ***Norms and Signals***

social norm for the group  $\varphi_k$  a threshold

types with  $y^i < \varphi_k$  expected to contribute

types with  $y^i > \varphi_k$  not expected to contribute

contributions are observable but types are private information

peers receive a noisy signal of the type

signal  $z^i$  continues to be 0 for “good, followed the social norm” and 1 for “bad violated the social norm”

supposed to contribute, so  $y^i < \varphi_k$  but did not do so then this is perfectly observed so that  $z^i$  takes the value 1 for sure.

did not contribute but was not supposed to contribute so  $y^i > \varphi_k$  then we assume that the signal is noisy so probability  $\pi$  that bad signal is received

## Structure of Costs

if the cost of the punishment to the individual is  $P^i$  then the cost to the group is  $\psi P^i$

$$\theta = \psi(1 - \pi); \underline{\varphi} = \max\{0, -d_0/\gamma\};$$

$$F = \max\{0, \gamma\theta d_0\} \text{ and } c = (\gamma/2)(1 - \underline{\varphi}) + F.$$

**Theorem:** *If  $\theta = 1/2$  then for  $\varphi^i < \underline{\varphi}$  we have the expected cost  $C(\varphi^i)$  strictly decreasing in  $\varphi^i$  and for  $\varphi^i > \underline{\varphi}$  we have  $C(\varphi^i) = F + c(\varphi^i - \underline{\varphi})$ .*

if  $\theta > 1/2$  (monitoring costly) then  $C$  is concave

if  $\theta < 1/2$  (monitoring cheap) then  $C$  is convex

Theorem 1 for the small group advantaged holds for  $C$  concave and for the large group advantaged holds for  $C$  convex

in general costly monitoring favors the small group and cheap monitoring the large group.

## Why not Split a Large Group?

with a positive fixed cost why doesn't the larger group “act like a smaller group” by appointing a smaller subgroup to act on its behalf?

a subgroup of size  $M_k < N_k$  will only receive a share of the prize:  
 $(M_k/N_k)V$

so raw willingness of the subgroup to pay is

$$M_k \underline{\varphi} + \frac{(M_k/N_k)V - M_k F}{c} = \frac{M_k}{N_k} \left( N_k \underline{\varphi} + \frac{V - N_k F}{c} \right) = \frac{M_k}{N_k} r_k$$

a fraction  $M_k/N_k$  of the raw willingness of the entire group to pay.

problem involves “renegotiation” subgroup will collude not to do it